

EST5104 Bayesian Inference

EST5803 Advanced Bayesian Inference

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Presentation

Start date: 06/08/2018

End date: 05/12/2018

Monday 14:00 - 16:00 ICMC-USP (Room 5-104)

Wednesday 14:00 - 16:00 ICMC-USP (Room 5-104)

Objectives

Develop Bayesian techniques for data analysis and interpretation.

Rationale

To understand how to combine past and present information to take decisions it is essential to discuss Bayesian principles.

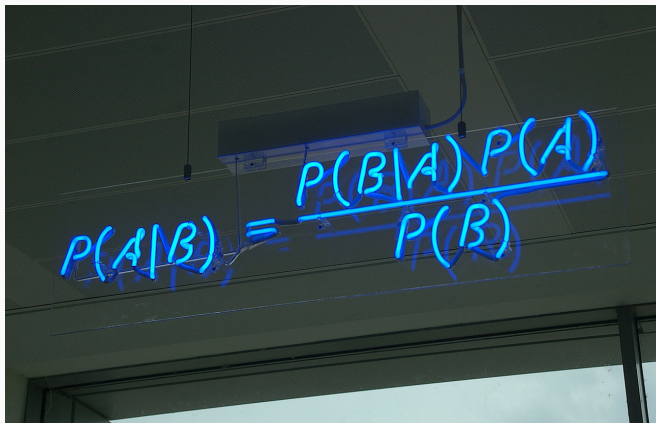
Content

1. Discussion on frequentist and bayesian statistical methods.
2. Basic concepts of the bayesian paradigm: Bayes theorem, prior and posterior probability distributions.
3. Subjective, Jeffreys, hierarchical and conjugate prior distributions.
4. Introduction to decision theory: loss functions, posterior decision analysis, bayesian parametric estimators.
5. Bayesian hypothesis tests. Hierarchical models.
6. Bayesian computations. Markov chain Monte Carlo methods.

The Reverend Thomas Bayes.



REV. T. BAYES

A photograph of a whiteboard with a blue marker equation. The equation is $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$. The whiteboard is mounted on a ceiling with a grid pattern. The lighting is dim, and the blue marker is the primary source of light in the scene.
$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

the theory 



that would



not die

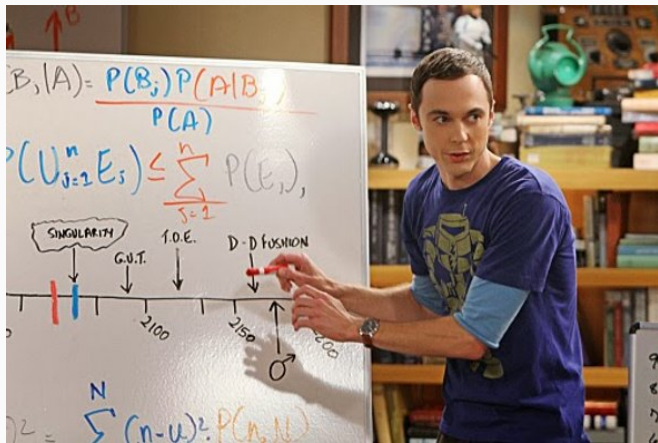


how bayes' rule cracked



the enigma code,





Bibliography

BERGER, J.O. Statistical Decision Theory and Bayesian Analysis. 2nd ed. Springer-Verlag. 1985.

Bernardo, J.M., Smith, A.F.M. Bayesian theory. New York: John Wiley and Sons, 1994.

CONGDON, P. Applied Bayesian Modelling. Second Edition. John Wiley & Sons, 2014.

GAMERMAN, D. & LOPES, H.F. Markov Chain Monte Carlo. Chapman & Hall, 2006.

GELMAN, A.; CARLIN, J. B.; STERN, H.S.; RUBIN, D.B. Bayesian Data Analysis. 2nd ed. Chapman & Hall, 2004.

OHAGAN, A. Bayesian Inference. Kendalls Advanced Theory of Statistics, vol. 2B. Arnold, London, 1994.

PAULINO, C.D.; TURKMAN, M.A.A. & MURTERA, B. Estatística Bayesiana. Fundação Calouste Gulbenkian – Lisboa, 2003.

**Springer Series
in Statistics**

James O. Berger

**Statistical
Decision Theory
and Bayesian
Analysis**

Second Edition



James O. Berger
Statistical Decision Theory and
Bayesian Analysis Springer, 1985.

Table of contents

CHAPTER 1: Basic Concepts

CHAPTER 2: Utility and Loss

CHAPTER 3: Prior Information and Subjective Probability

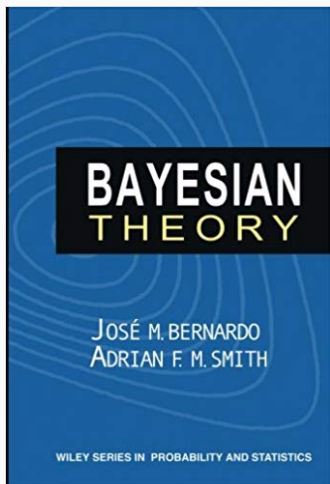
CHAPTER 4: Bayesian Analysis

CHAPTER 5: Minimax Analysis

CHAPTER 6: Invariance

CHAPTER 7: Preposterior and Sequential Analysis

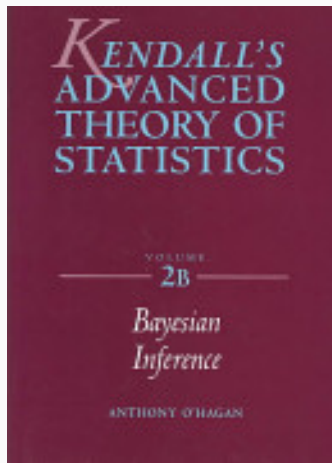
CHAPTER 8: Complete and Essentially Complete Classes



Bernardo, J.M., Smith, A.F.M.
Bayesian Theory. New York: John
Wiley and Sons, 1994.

Table of contents

1. INTRODUCTION
2. FOUNDATIONS
3. GENERALISATIONS
4. MODELLING
5. INFERENCE
6. REMODELLING



Anthony O'Hagan
Kendall's Advanced Theory of
Statistics: Bayesian inference.
Volume 2B, Volume 2, Parte 2 Ed-
ward Arnold, 1994

Table of contents

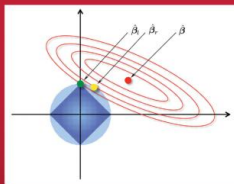
- 1 The Bayesian method
- 2 Inference and decisions
- 3 General principles and theory
- 4 Subjective probability
- 5 Non-subjective theories
- 6 Subjective prior distributions
- 7 Robustness and model comparison
- 8 Computation
- 9 The Linear Model
- 10 Other Standard Models

Texts in Statistical Science

Statistical Inference

An Integrated Approach

Second Edition



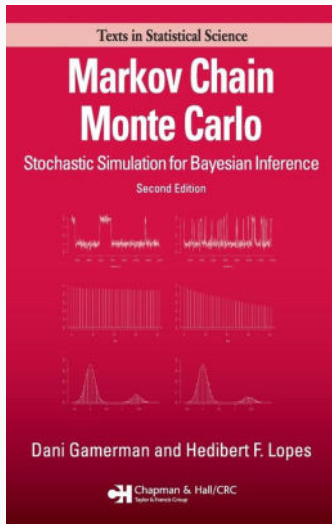
Helio S. Migon
Dani Gamerman
Francisco Louzada

 CRC Press
Taylor & Francis Group
A CHAPMAN & HALL BOOK

Helio S. Migon, Dani Gamerman,
Francisco Louzada
Statistical Inference: An Inte-
grated Approach, Second Edition
Chapman and Hall/CRC, 2014

Table of Contents

- 1 Introduction
- 2 Elements of Inference
- 3 Prior Distribution
- 4 Estimation
- 5 Approximating Methods
- 6 Hypothesis Testing
- 7 Prediction
- 8 Introduction to Linear Models



Dani Gamerman & Hedibert
Lopes
Markov Chain Monte Carlo:
Stochastic Simulation for
Bayesian Inference (Second
Edition) Chapman & Hall, 2006

Table of Contents

Chapter 1. Stochastic simulation

Chapter 2. Bayesian inference

Chapter 3. Approximate methods of inference

Chapter 4. Markov chains

Chapter 5. Gibbs sampling

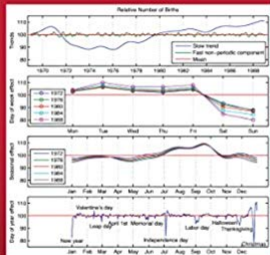
Chapter 6. Metropolis-Hastings algorithms

Chapter 7. Further topics in MCMC

Texts in Statistical Science

Bayesian Data Analysis

Third Edition



Andrew Gelman, John B. Carlin, Hal S. Stern,
David B. Dunson, Aki Vehtari, and Donald B. Rubin

 **CRC Press**
Taylor & Francis Group
A CHAPMAN & HALL BOOK

Andrew Gelman, John B. Carlin,
Hal S. Stern, David B. Dunson,
Aki Vehtari, Donald B. Rubin
Bayesian Data Analysis (Third
Edition) Chapman and Hall/CRC,
2013

Table of Contents

Part I: Fundamentals of Bayesian Inference

- 1 Probability and inference
- 2 Single-parameter models
- 3 Introduction to multiparameter models
- 4 Asymptotics and connections to non-Bayesian approaches
- 5 Hierarchical models

Part II: Fundamentals of Bayesian Data Analysis

- 6 Model checking
- 7 Evaluating, comparing, and expanding models
- 8 Modeling accounting for data collection
- 9 Decision analysis

Part III: Advanced Computation

- 10 Introduction to Bayesian computation
- 11 Basics of Markov chain simulation

- 12 Computationally efficient Markov chain simulation
- 13 Modal and distributional approximations

Part IV: Regression Models

- 14 Introduction to regression models
- 15 Hierarchical linear models
- 16 Generalized linear models
- 17 Models for robust inference
- 18 Models for missing data

Part V: Nonlinear and Nonparametric Models

- 19 Parametric nonlinear models
- 20 Basis function models
- 21 Gaussian process models
- 22 Finite mixture models
- 23 Dirichlet process models

Computational Resources



The R Project for Statistical Computing



The Stan Project for high-performance statistical computation

JAGS

Just Another Gibbs Sampler

Societies



**International Society for
Bayesian Analysis**



**American Statistical
Association, Section
on Bayesian Statistical
Science**

EST5104 - Bayesian Inference

Credits: 7

2 written examinations, $P1$ and $P2$. Final grade (NF) will be computed as,

$$NF = (2P1 + 3P2)/5$$

EST5803 - Advanced Bayesian Inference

Credits: 10

2 written examinations, $P1$ and $P2$. Final grade (NF) will be computed as,

$$NF = (3P1 + 3P2 + T)/7$$

where T is the average of home works.